

# L02: Cryptographic Foundations

BSc Blockchain Course

Digital Finance

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## By the end of this lesson, you will be able to:

- 1 Explain the properties of cryptographic hash functions
- 2 Describe how digital signatures provide authentication
- 3 Understand elliptic curve cryptography basics (ECDSA)
- 4 Explain how Merkle trees enable efficient verification
- 5 Derive a blockchain address from a public key

*These primitives are the foundation of all blockchain security.*

## Four Key Properties

- Deterministic: Same input always yields same output
- One-way: Cannot reverse to find input
- Collision resistant: Hard to find two inputs with same output

### Four Key Properties of Cryptographic Hash Functions

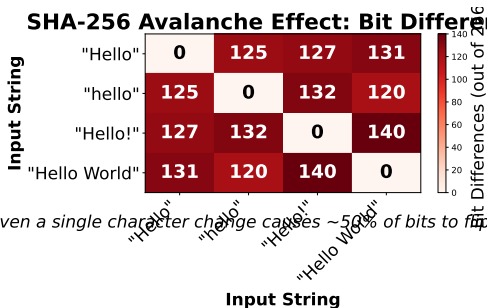


Same input always gives same output  
Cannot reverse to find input  
Hard to find two inputs with same output  
Small change in input = big change in output

Example: `SHA-256("Hello") = 185f8db32271fe25f561a...`

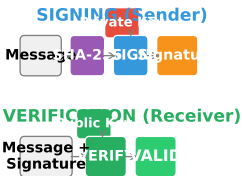
*SHA-256 (Bitcoin) and Keccak-256 (Ethereum) are the primary hash functions.*

## SHA-256 Avalanche Effect: Bit Differences



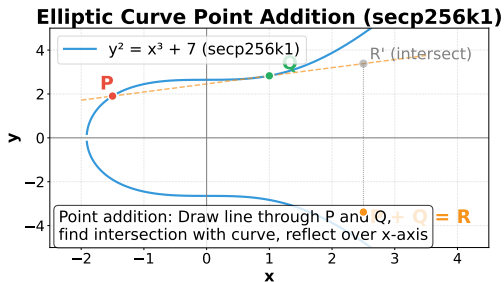
Even a single character change causes ~50% of bits to flip (128 bits)

*A single bit change causes approximately 50% of output bits to flip.*



Private key signs, public key verifies. Only the owner can sign, anyone can verify.

Private key signs; public key verifies. Only owner can sign.



*secp256k1 curve used by Bitcoin and Ethereum. Point addition is the core operation.*

*Private key -> Public key (easy) | Public key -> Private key (impossible)*

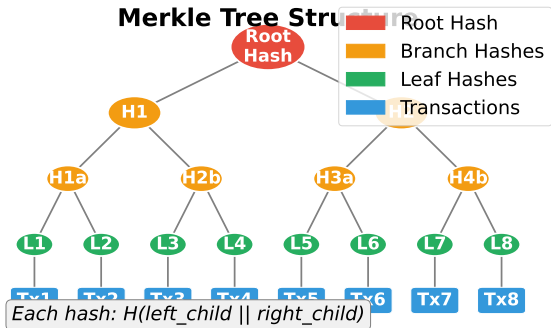
## Key Generation Process



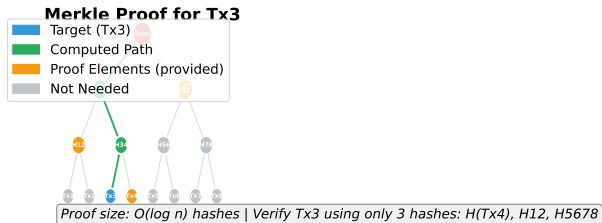
256 bits of entropy  
Keep secret  
Never share  
 $k * G$   
512 bits coordinates  
Hash + checksum

**PRIVATE (keep secret)** | **PUBLIC (share freely)**

*Private key to public key is easy; reverse is computationally infeasible.*



Binary hash tree enables  $O(\log n)$  transaction verification.



*Light clients can verify transactions without downloading entire blocks.*

## Remember These Points

- 1 Hash functions provide integrity and link blocks together
- 2 Digital signatures prove ownership without revealing private keys
- 3 ECDSA enables compact signatures (64 bytes vs RSA 256+)
- 4 Merkle trees allow efficient verification in  $O(\log n)$
- 5 Addresses are derived from public keys via hashing

**Next Lesson:** Bitcoin Deep Dive – UTXO model, mining, and transaction structure.